

Quantitative Modeling of Spatio-temporal Dynamics of Inferior Olive Neurons with a Simple Conductance-based Model

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Abstract

Inferior olive (IO) neurons project to the cerebellum and contribute to motor control. They can show intriguing spatio-temporal dynamics with rhythmic and synchronized spiking. IO neurons are connected to their neighbors via gap junctions to form an electrically coupled network, and it is thought that this coupling contributes to the characteristic dynamics of this nucleus. Here we demonstrate that a gap junction-coupled network composed of simple conductance-based model neurons (a simplified version of a Hodgkin-Huxley type neuron) reproduce important aspects of IO activity. The simplified phenomenological model neuron facilitated the analysis of the single cell and network properties of the IO while still quantitatively reproducing the spiking patterns of complex spike activity observed by simultaneous recording in anesthetized rats. The results imply that both intrinsic bistability of each neuron and gap junction coupling among neurons play key roles in the generation of the spatio-temporal dynamics of IO neurons.

Keywords: Inferior olive, Cerebellum, Gap junction, Synchronization, Bifurcation analyses.

1 Introduction

The axons of inferior olive (IO) neurons end as climbing fibers on cerebellar Purkinje cells, whose axons in turn comprise the only output from the cerebellar cortex. Each Purkinje cell receives input from only one climbing fiber, and activation of its climbing fiber evokes a high frequency burst of action potentials, known as a complex spike (CS) in the Purkinje cell [Eccles *et al.*, 1966]. IO neurons fire (and therefore CSs occur) at a very low average rate of about 1 Hz. CS activity is also characterized by a transient rhythmicity with about 10Hz and a tendency for synchronization [Lang *et al.*, 1999; Sasaki *et al.*, 1989]. CS activity has been hypothesized to play such roles in motor control as contributing to the timing of motor commands [Welsh *et al.*, 1995] and relaying an error detection signal

[Kawato & Gomi, 1992; Schweighofer *et al.*, 1998]; however, its exact roles remain a controversial subject in part because of the unusual firing properties just described. Moreover, these characteristics of olivocerebellar activity, namely, rhythmicity and synchronicity, should be incorporated into the various hypotheses concerning the roles of the IO in motor control and cerebellar learning, but typically are not.

Understanding the mechanisms by which rhythmic and synchronous CS activity patterns are generated may aid in remedying this situation, yet these mechanisms have only begun to be explored. Synchronous CS activity was proposed to be due to gap junction-mediated electrical coupling between IO neurons [Llinas *et al.*, 1974]. Evidence strongly supporting this hypothesis has been obtained recently [Blenkinsop & Lang, 2006; Lang, 2001; Marshall *et al.*, 2007]. In contrast, the low firing rate and rhythmicity of CSs are thought to originate from the intrinsic properties of IO neurons [Llinas & Yarom, 1981b; Llinas & Yarom, 1981a], particularly because rhythmic activity also can be observed at a sub-threshold level in neurons in slices of the IO [Bal & McCormick, 1997; Benardo & Foster, 1986; Llinas & Yarom, 1986]. However, gap junction coupling may contribute to the firing rates of IO neurons [Blenkinsop & Lang, 2006], and also may be required for rhythmic IO activity, but this still remains a controversial issue [Bleasel & Pettigrew, 1992; Blenkinsop & Lang, 2006; Lampl & Yarom, 1997; Leznik & Llinas, 2005; Llinas & Yarom, 1986; Long *et al.*, 2002; Manor *et al.*, 1997; Marshall *et al.*, 2007; Placantonakis *et al.*, 2006]. Indeed, little is known about how gap junction coupling interacts with the other membrane conductances of the neurons to give rise to the dynamics of IO activity.

Mathematical modeling may be useful for exploring the underlying mechanisms of the spatio-temporal dynamics of IO neurons, but selection of a proper model is a key issue. One approach to studying neuronal dynamics is to focus on the structural and physiological details of individual neurons, as is, for example, done in building multicompartment models of neurons based on dynamics of different kinds of ion channels and dendritic tree structures. Such physiologically realistic models replicate the details of the activity of individual neurons. However, such models require solving high-dimensional systems of equations, and when trying to simulate a network of cells it can be hard to define the

underlying dynamics that are displayed by such models. Another approach is to simplify the individual model neurons, but still have a network that displays the core features of the activity of the modeled system. Two-variable conductance-based models, which have been well investigated, are often suitable for this purpose [Izhikevich, 2006].

In previous modeling studies of IO neurons, the sub-threshold oscillation that these cells display has been replicated using two-variable models [Manor *et al.*, 1997]. In addition, several spiking patterns can be realized using a two-compartment (soma and dendrite) model of an IO neuron [Schweighofer *et al.*, 1999]. However, neuronal gap junction density in the IO is among the highest in the adult CNS [Belluardo *et al.*, 2000; Condorelli *et al.*, 1998], and thus electrical coupling likely is a key factor for determining the dynamics of IO neuronal activity. Here, we show that a system composed of simple two-variable conductance-based model neurons coupled by gap junctions quantitatively reproduces the spatio-temporal dynamics of CS activity that was recorded from multiple Purkinje cells simultaneously. Furthermore, phase plane and bifurcation analyses demonstrated that the model IO network has intrinsic bistability, which suggests that this property may play a key role in shaping the characteristic activity of IO neurons.

2 Methods

2.1 Experimental data

The data used to constrain the quantitative modeling were simultaneous recordings of CS activity from crus 2a Purkinje cells in anesthetized adult female Sprague-Dawley rats. Because each CS in a Purkinje cell is evoked by the firing of a single IO neuron and each IO discharge causes a CS, the firing of IO neurons can be represented by that of CSs in Purkinje cells. One should note that spontaneous CS activity patterns under ketamine-xylazine anesthesia are similar to those in awake animals, so the system appears to be operating within its normal physiological range [Lang *et al.*, 1999].

Recording procedures. Experiments involving animals were carried out in accordance with the National Institutes of Health guidelines for the care and use of laboratory animals. Experimental protocols were approved by the IACUC committee of New York University School of Medicine. Detailed descriptions of the surgical and recording procedures have already been published [Sasaki *et al.*, 1989]. In brief, Sprague-Dawley rats (225-300 gm) were anesthetized with an intraperitoneal injection of ketamine (100 mg/kg) and xylazine (8 mg/kg). Supplemental anesthetic doses were given to prevent spontaneous and reflex movements. Rectal temperature was maintained at 36-37°C by an electric heating pad. Animals were mechanically ventilated, and given supplemental oxygen when necessary. Following anesthetization, the bone, dura, and overlying tissues were removed to expose the cerebellar cortex, which was then covered by a platform that allowed access to lobule crus 2a. Glass micro-electrodes (~1 MΩ) were inserted through the platform and into the cerebellar cortex using a joy-stick-controlled piezoelectric micromanipulator (Burleigh Instruments, NY). Each micro-electrode was positioned to record CS activity from a single Purkinje cell. The data used in this paper were collected in two experiments using either a 6 x 4 or 10 x 4 (mediolateral x rostrocaudal) rectangular array of electrodes, with an inter-electrode spacing of 250 μm. In one experiment 16 of 24 electrodes showed well-isolated CS activity, and in the other 22 of 40 electrodes did. CSs were viewed on an oscilloscope, and their times of occurrence were recorded using a multichannel amplifier system (1000x gain, 6 kHz per channel sampling rate) with a single voltage level threshold. Following electrode implantation, a control recording of spontaneous CS activity was obtained. Next, an injection pipette was lowered to the IO and either a pressure injection of picrotoxin (1 mg/ml in Ringers or saline, ~1μL/min) or carbenoxolone (500 μM in Ringers, 0.1 μL/min) was made.

2.2 Statistical analyses

To ensure that the model was robust, that is to increase the likelihood that its dynamics would reflect some general principles of the IO rather than the dynamics of a

particular condition, the model was required to reproduce the spatio-temporal dynamics of the olivocerebellar system under three different conditions (four experimental data sets): before (control) and after an injection of picrotoxin, a gamma-aminobutyric acid-A (GABA_A) antagonist, and before (control) and after an injection of carbenoxolone, a gap junction antagonist that blocks electrical coupling of IO neurons. The data from the injections of picrotoxin and the carbenoxolone were collected in separate experiments.

To assess how closely the simulated data produced by the model and the experimental data correspond, both were characterized using several measures of population activity, including population auto- and cross-correlograms, and the minimal distance distribution, which are described below.

Population auto- and cross-correlograms. To generate population correlograms, auto- or cross-correlograms were calculated for all neurons and pairs of neurons, respectively, and then averaged. The mean and standard deviation of each histogram bin was determined using the appropriate population (all neurons and all cell pairs). Population auto- and cross-correlograms were then obtained from these average correlograms by normalizing the latter such that the sum of all bins in a correlogram equaled unity.

Minimal Distance Distribution. To visualize the difference between the spike data and a random process, the minimal distance distribution was used (Figs. 1f, 1j and Figs. 2f, 2j). The minimal distance between the k th spike of neuron i and a spike of neuron j is given as follows:

$$s_k^{i,j} = 1 - \exp\left(\frac{-2 \min_m |t_k^i - t_m^j|}{\bar{d}^j}\right), \quad (1)$$

where t_k^i is the k th spike time of neuron i ; \bar{d}^j is the mean interspike interval of neuron j ; and m runs from 1 to the total number of spikes by neuron j . If spike k is synchronous with a spike in neuron j , the quantity $s_k^{i,j}$ equals zero. If the minimal interval between spike k and any spike in neuron j is large relative to \bar{d}^j , the quantity $s_k^{i,j}$ will be

close to one. Note that $s_k^{i,j}$ is normalized so that if the spike sequence is a random process (Poisson point process), then $s_k^{i,j}$ will be distributed uniformly between 0 and 1. Thus, the difference from the uniform distribution can be regarded as that from a Poisson process.

The statistical measures described below were used for assessing the effect of varying the parameters of the model on basic characteristics of CS activity, namely firing rates, synchrony and rhythmicity.

In the present paper, the following measure of rhythmicity was defined. Suppose that $\{T_1, T_2, \dots, T_n\}$ is a consecutive sequence of interspike intervals, then the rhythmicity of that cell is defined as follows:

$$1 - \frac{1}{n-1} \sum_i^{n-1} \frac{3(T_i - T_{i+1})^2}{(T_i + T_{i+1})^2}, \quad (2)$$

where the second term is the local variance which is known as a measure of irregularity [Shinomoto *et al.*, 2005]. When rhythmic activity occurs, successive interspike intervals are equal or nearly so. In the case of a highly rhythmic cell, many of the terms in the summation will be equal to or close to zero, and the rhythmicity value will approach unity. In contrast, if the spike sequence is a Poisson random point process, the rhythmicity will equal to zero.

To quantify the degree of synchrony, we computed a correlation coefficient of spike trains [Lang *et al.*, 1996]. The spike train of the i th neuron was represented $x_i(k)$, where k represents the time step ($k = 1, 2, \dots, K$). $x_i(k)=1$ if the CS occurred in the k th time bin, otherwise $x_i(k)=0$. We set the bin width to be 10 ms. The synchrony between neuron i and neuron j was calculated as

$$\frac{\sum_{k=1}^K y_i(k) \cdot y_j(k)}{\sqrt{\sum_{k=1}^K y_i(k)^2 \cdot \sum_{k=1}^K y_j(k)^2}}, \quad (3)$$

where $y_i(k)$ is the normalized forms of $x_i(k)$:

$$y_i(k) = x_i(k) - \frac{1}{K} \sum_{l=1}^K x_i(l). \quad (4)$$

2.3 The model

We simulated an IO-like network by making a model consisting of electrically-coupled simplified neuronal elements. Each neuron was modeled as a simple two-variable conductance-based element, which nevertheless could generate many of the features of single neurons [Izhikevich, 2006]. The model can be viewed as a reduced Hodgkin-Huxley (HH) model [Hodgkin & Huxley, 1952]. In their pioneering work, Hodgkin and Huxley found that the neuronal dynamics of a squid giant axon could be well described with 3 main currents: an ohmic leak current and voltage-gated sodium and potassium currents, the latter two of which depolarize and hyperpolarize the membrane potential, respectively. They showed that the nonlinear dynamics of these currents allows for the generation of action potentials by the model axon. The HH model includes 4 variables: the membrane potential and 3 variables related to ion channel activation and inactivation. In contrast, the present model uses two variables: the membrane potential V and the activation of an ion channel n . These variables are governed by the following equations [Izhikevich, 2006]:

$$C \frac{dV}{dt} = I - g_L(V - E_L) - g_D m(V)(V - E_D) - g_H n(V - E_H), \quad (5)$$

$$\tau_n \frac{dn}{dt} = n_\infty(V) - n, \quad (6)$$

where $C = 1\mu\text{F}/\text{cm}^2$ is the membrane capacitance; g_L , g_D , and g_H are the conductances of ion channels for the leak, depolarizing, and hyperpolarizing currents, respectively; and E_L , E_D , and E_H are the corresponding reversal potentials. We choose following parameters so that the model shows a subcritical Hopf bifurcation and that these parameters are in biologically plausible range [Schweighofer *et al.*, 1999]. For the second term on the right side of the Eq. (5), we set $g_L = 0.05 \text{ mS}/\text{cm}^2$ and $E_L = -78 \text{ mV}$ for the

leak current. For the third term, we set $g_D = 0.05 \text{ mS/cm}^2$ and $E_D = 120 \text{ mV}$ for the depolarizing current. The function $m(V)$ depends on V and represents the level of activation of the depolarizing current. The activation of the voltage-dependent channel is represented as

$$m(V) = \frac{1}{1 + \exp[(V_1 - V)/V_2]}. \quad (7)$$

This activation curve is specified with $V_1 = -60 \text{ mV}$ and $V_2 = 5 \text{ mV}$. We set $g_H = 0.2 \text{ mS/cm}^2$ and $E_H = -100 \text{ mV}$ for the hyperpolarizing current. The dynamics of n is specified with a time constant τ_n and a steady state function $n_\infty(V)$ defined as

$$n_\infty(V) = \frac{1}{1 + \exp[(V_3 - V)/V_4]}, \quad (8)$$

where we set $V_3 = -70 \text{ mV}$ and $V_4 = 5 \text{ mV}$.

Using this neuron model as a basic building block, we constructed a network of 25 neurons coupled with gap junctions as a model of the IO system. Each neuron is driven by an external input I_i^{ext} and three types of currents as follows.

$$C \frac{dV_i}{dt} = I_i^{ext} - g_L(V_i - E_L) - g_D m(V_i)(V_i - E_D) - g_H n_i(V_i - E_H), \quad (9)$$

where V_i is the membrane potential of the i th neuron. The activation dynamics of the hyperpolarizing channel of the i th neuron n_i is represented by the following equation:

$$\tau_n \frac{dn_i}{dt} = n_\infty(V_i) - n_i. \quad (10)$$

The external current I_i^{ext} consists of the constant current I_0 , the fluctuating input $\xi_i(t)$, and the current induced with the gap junctions as follows:

$$I_i^{ext} = I_0 + \xi_i(t) - g_G \sum_j^{neighbors} (V_i - V_j). \quad (11)$$

The IO is innervated both by excitatory terminals, derived from either ascending or descending inputs, and by inhibitory GABAergic terminals, derived mainly from the cerebellar nuclei [Nelson & Mugnaini, 1989; Sotelo *et al.*, 1986]. Both the excitatory and inhibitory terminals can be divided into two classes based on their site of termination on IO neurons. Roughly half of the terminals (both excitatory and inhibitory) synapse onto the main dendrites or soma [de Zeeuw *et al.*, 1989]. Such synapses are likely to affect the overall excitability of an IO neuron. Thus, the effects of this first class of synapses (those onto the main dendrites and soma) were modeled by the constant and variable input currents, I_0 and $\xi_i(t)$, where I_0 was applied equally to all neurons, and $\xi_i(t)$ was generated using Gaussian white noise with standard deviation σ , and was applied to each neuron independently at every integration time step of 0.05 ms. Note that by using a single parameter, I_0 , for the level of constant synaptic input, we are treating loss of inhibition as equivalent to an increase in excitatory synaptic input.

The other approximately half of the IO terminals synapse onto the dendritic spines adjacent to gap junctions that connect the spines of neighboring IO neurons [de Zeeuw *et al.*, 1989; Sotelo *et al.*, 1986], as shown schematically in Fig. 3a. These synapses, because of their locations, are typically thought to affect primarily the effective coupling between IO neurons. This modulation in effective electrical coupling is not due to the transmitter acting directly on the gap junction itself, but rather to its increasing the conductance of the spine membrane adjacent to the gap junction [Llinas *et al.*, 1974]. By changing the conductance of the spine membrane these synapses will selectively alter the amount of current flowing across a specific gap junction without significantly altering the overall membrane properties of the cell. Thus, particularly in terms of the phenomenological model used in this paper, modulating the conductance of the spine membrane will have an equivalent but inverse effect on electrical coupling as modulating the gap junction conductance directly. That is, an increase in spine membrane conductances by transmitter release would be equivalent to reducing the gap junction conductance: in both cases a smaller fraction of the current will flow across the gap junction and therefore there will be a decrease in electrical coupling between the cells connected by the gap junction.

In order to model the electrical coupling via gap junctions in IO, we assumed that each neuron is randomly coupled to other neurons with a probability of 20%, and that for a given experimental condition (control, picrotoxin, carbenoxolone), the effective conductance of the connection, g_G , is the same for all cell pairs that are coupled. Thus, the summation in Eq. (11) runs over all gap junction-coupled neurons, and the magnitude of the current flowing between two cells was determined from their potential difference and the effective conductance between them.

To approximately estimate the effective coupling conductance between two IO neurons, the equivalent circuit shown in Fig. 3b was used as a model of two IO neurons coupled via the gap junction between two dendritic spines on which GABAergic synapses are formed. If g_{GABA} , g_{GJ} , and g_{DS} are conductances of the GABAergic synapses, the gap junction, and the dendritic spines respectively, the current I_{GJ} and effective conductance, g_G , between two neurons are described as follows:

$$I_{GJ} = \frac{g_{GJ} \cdot g_{DS}}{2g_{GJ} + g_{DS} + g_{GABA}} \cdot (V_1 - V_2) = g_G \cdot (V_1 - V_2) \quad (12)$$

According to this equation, it can be seen that picrotoxin increases the effective conductance g_G between the two neurons by decreasing g_{GABA} , the conductance due to the GABAergic synapses on the spine membrane. In contrast, carbenoxolone reduces the effective conductance g_G by directly decreasing the conductance of the gap junction g_{GJ} . Although the mechanisms by which these drugs act are distinct, the functional effects in terms of the coupling strength in IO network are opposite (i.e., opposite changes in the effective coupling conductance between two neurons). Thus, for the sake of simplicity, we replaced the equivalent circuit in Fig. 3b by an approximate circuit model shown in Fig. 3c, in which a single element represents the effective coupling conductance between two IO neurons.

2.4 Parameter estimation

The parameters were determined so that the model quantitatively reproduced the experimental spiking pattern. The unknown parameters that were estimated are the magnitude of the constant input, I_0 ; the intensity of fluctuating input, σ ; and the effective conductance of gap junction, g_G . Although, one of our interests was to evaluate how the injection of picrotoxin or carbenoxolone affected these parameters, we also wanted to estimate the time constant, τ_n , which is highly sensitive to the periodicity of the neuronal firing. Therefore, the estimation procedure was first done by using a dataset which shows more periodic activity in each experiment: the picrotoxin dataset in the picrotoxin experiment and the control dataset in the carbenoxolone experiment. Then τ_n was fixed to keep the periodicity, and the values of the other parameters were estimated again, using the less periodic dataset.

To obtain a criterion for the goodness of the parameter estimation, we used the following statistics of the spiking patterns: the firing rate, the minimal distance distribution, and the auto- and cross-correlogram distributions. The estimation was performed by minimizing the differences of these statistics between the experimental data and the simulation result as follows. The summed difference function, D_{total} , consisted of four terms, each of which is based on the statistics of the spiking patterns:

$$D_{total} = D_{MD} + D_{AC} + D_{CC} + \rho D_{FR}. \quad (13)$$

The first term D_{MD} is the mean square error (MSE) of the minimal distance distribution. The second and third terms are the MSEs of the auto- and cross-correlograms. The quantity D_{FR} is the difference of mean firing rates divided by the mean experimental firing rate, $D_{FR} = |f_{model} - f_{data}| / f_{data}$, where f_{model} and f_{data} are the mean firing rates of the simulated neurons and that of the experimentally recorded cells, respectively. ρ is a coefficient that weights the contribution of D_{FR} . We choose $\rho = 1 \times 10^{-4}$ so that the amount and change of D_{FR} are nearly equal to these of other distances. In order to minimize D_{total} ,

the Neelder-Mead method [Nelder & Mead, 1965] was used. The duration of the simulation was set as 1000 s.

3 Results

3.1 Population Statistics of the Experimental Data.

The effects of picrotoxin and carbenoxolone on CS activity have been reported previously. Picrotoxin was shown to increase the CS firing rate, synchrony, and rhythmicity [Lang, 2002; Lang *et al.*, 1996]. Carbenoxolone had much the opposite effect, reducing the CS firing rate, synchrony, and rhythmicity [Blenkinsop & Lang, 2006]. Here, the data from two experiments that were part of those studies were analyzed using the statistical measures of population activity that were described in Methods (Sec. 2.2).

The patterns of CS activity in the picrotoxin experiment are illustrated in raster displays in Fig. 1. The spiking pattern of the control condition has a mean firing rate of 1.13 ± 0.67 Hz, typical of CS activity. Significant correlations do exist for the activity of some cell pairs, particularly those pairs in which both cells are located within the same rostrocaudally running strip of cortex [Lang *et al.*, 1999; Sasaki *et al.*, 1989], but such correlations are hard to detect in the raster format (Fig. 1a), because the activity of most cells are not correlated. After picrotoxin injection, the average firing rate (2.09 ± 1.10 Hz), synchrony, and rhythmicity all increased significantly, and correlated activity among the cells is easily observable in the picrotoxin rasters. Further, the CS activity shows a pattern of switching between a rhythmic synchronous spiking state and a desynchronized state (Fig. 1b).

The picrotoxin-induced changes in CS activity can be demonstrated more clearly by using statistical distributions that characterize the spiking patterns (Fig. 1c-j). Auto-correlograms of a typical cell recorded before and after picrotoxin injection are shown in Figs. 1c, g. The pre-injection auto-correlogram shows one peak at ~ 100 ms, which is indicative of the tendency of CS rhythmicity to occur at a frequency of about 10 Hz.

Picrotoxin injection greatly enhanced the rhythmicity, which is indicated by the many peaks in the auto-correlogram, and lengthened the oscillation period to ~180 ms.

In the case of this dataset, the pre-injection population auto-correlogram (Fig. 1d) does not show a prominent peak at ~100 ms, which partly reflects a relatively low rhythmicity in this set of cells, but also that Purkinje cells at different cortical locations display CS activity with somewhat different oscillation frequencies [Sasaki *et al.*, 1989], leading to smearing of the peaks in the single cell autocorrelograms into a shallow, indistinct, and broad hump in the population autocorrelogram. After picrotoxin injection, however, the population autocorrelogram shows multiple peaks, which reflects both an increase in the rhythmicity of individual cells and a greater uniformity of the oscillation frequencies across the population (Fig. 1h). The pre-injection population cross-correlogram (Fig. 1e) had a peak at 0 ms, indicating synchronous CS activity among at least some Purkinje cells. Injection of picrotoxin into the IO greatly enhanced the level of synchrony (Fig. 1i).

The effect of picrotoxin was also apparent using the MDD statistic. In the control condition, most of the distribution for the CS activity is flat, however, the bins near zero are higher than the baseline, which indicates the existence of synchronization at higher than chance levels among at least some of the cells. In the picrotoxin condition, the zero and neighboring bins in the minimal distance distribution are much higher than the baseline or than the corresponding values for the control condition, consistent with previous correlational analyses showing increased synchronization of CS activity following injection of picrotoxin [Lang *et al.*, 1996; Lang, 2002]. Surprisingly, under picrotoxin there is also an increase in the height of the bins at the upper end of the distribution, leading to a bimodal distribution. This second peak indicates that desynchronized states (i.e., less simultaneous spikes than expected by chance) also occurred. Thus, in the picrotoxin condition, CS activity seems to cycle between synchronous and asynchronous states, as can be seen in the raster plot (Fig. 1b). It will be shown below that the model can reproduce both the changes in the correlograms and in the MDD distribution (unimodal to bimodal) that were induced by picrotoxin.

Statistical analysis of the spiking pattern of the control condition in the carbenoxolone experiment, like the control condition of the picrotoxin experiment, showed that synchronous spiking was limited to a few cell pairs, and that CS activity had a mean firing rate of 1.02 ± 0.70 Hz (Fig. 2a, c-f). After injection of carbenoxolone, the mean firing rate (0.58 ± 0.43 Hz), synchrony levels, and rhythmicity all decreased significantly (Fig. 2b, g-j). Specifically, the number and height of the peaks in auto- and cross-correlograms and in the minimal distance distribution all are decreased by carbenoxolone. This suggests that gap junction coupling is important for both the rhythmicity and synchrony of CS activity.

3.2 Matching of simulated data and parameter estimation of the model

Figures 4 and 5 show that the model behavior with the estimated parameter values found by minimizing D_{total} reproduces the patterns shown by the experimental data in each experimental condition. For example, in control, the spikes of most neurons in the network are uncorrelated, with only a limited number of cells showing synchronous CS activity (Figs. 4a and 5a), whereas in the simulation of the picrotoxin condition, the model generates activity that switches between a rhythmic synchronously spiking state and an asynchronously spiking state (Fig. 4b).

The population statistical distributions generated from the model data are in good agreement with those from the experimental data, except for the control population autocorrelogram in the picrotoxin experiment (Figs. 4c-h and 5c-h). In this one exception, the model population autocorrelogram had a primary peak that was absent from the autocorrelogram from the experimental data (Fig. 4c); however, as already mentioned, the absence of the peak in the control population autocorrelogram from the experimental data is unusual in that a peak is often observed, as in the control population autocorrelogram from the carbenoxolone experiment.

The estimated parameter values are summarized in table 1. In the picrotoxin experiment, the I_0 and g_G are increased, and σ is decreased by the injection of

microtoxin. In the carbenoxolone experiment, on the other hand, I_0 , g_G , and σ are all decreased by the injection of carbenoxolone. Figure 6 shows the dependence of the summed difference function D_{total} on those parameters and suggests that the obtained parameter value locates on a minimum of D_{total} and is a unique solution for the parameter space.

3.3 Phase plane and bifurcation analyses

Once the model accurately reproduced the experimental data in both conditions, phase plane and bifurcation analyses were used to clarify the differences in spatio-temporal dynamics of the model network. First, we considered the single-neuron dynamics in the absence of fluctuating input and gap junction coupling by illustrating the $V-n$ trajectory on the two-dimensional phase plane.

In the case of the control condition (see Figs. 7a, 8a, and 9a), the trajectory in the phase plane converges to the stable equilibrium point, which corresponds to the resting state. In the resting state, if the neuron receives a weak stimulation, only a small perturbation of the membrane potential is produced, and the system quickly returns to the resting state. In contrast, a sufficiently strong stimulus induces a large excursion of the system's state that corresponds to the genesis of an action potential. Fig. 8a indicates that, in the control condition, action potentials are generated only by pulse current inputs whose amplitudes are 0.4 and 0.5 mA/cm².

On the other hand, in the microtoxin condition (Figs. 7b and 8b), two attractors co-exist: the stable equilibrium point (the resting state) and the stable limit cycle that corresponds to a periodically spiking state (Fig. 7b). If the orbit starts at a point inside of an unstable limit cycle (the blue dashed curve in Fig. 7b), the orbit converges to the stable equilibrium. On the contrary, if the orbit starts from a point outside the unstable limit cycle, it converges to the stable limit cycle. These two attractors, i.e., the resting and periodically spiking states, are realized under the same magnitude of the constant input. This bistability is a key to explaining the activity of IO neurons. Fig. 8b indicates that pulse inputs of amplitude 0.3 mA/cm² induce the switching between the two states depending on the

timing of the input. That is, the system can jump from one attractor to the other and vice versa if inputs of appropriate magnitude are given to the system.

How this qualitative difference of neuronal dynamics depends on the magnitude of the constant input, I_0 , is depicted in the bifurcation diagram (Fig. 7c). The input magnitude estimated using the control condition data is relatively low, as indicated by the left vertical line in Fig. 7c. In the range of such small I_0 , the resting state is the unique attractor. When the magnitude of I_0 increases and reaches $I_0 = 1.637 \mu\text{A}/\text{cm}^2$, a pair of stable and unstable limit cycles appears through a saddle-node bifurcation. The input magnitude of the picrotoxin condition corresponds to the situation with $I_0 = 1.641 \mu\text{A}/\text{cm}^2$. Further, at $I_0 = 1.90 \mu\text{A}/\text{cm}^2$, the unstable limit cycle shrinks to an unstable point, the same one at which there had been a stable equilibrium. Thus for $I_0 \geq 1.90 \mu\text{A}/\text{cm}^2$ the trajectory of the system will always converge to the stable limit cycle regardless of the starting point. This type of qualitative change in the dynamics of a system as the value of the constant input I_0 is varied is a subcritical Hopf bifurcation. To test whether the system could show other types of dynamics, such as a supercritical Hopf bifurcation or a homoclinic bifurcation, the model was run using a variety of sets of parameter values. However, the model did not display other types of dynamics while maintaining good agreement with the experimental data.

In contrast to picrotoxin, carbenoxolone did not cause a qualitative change of the phase plane and the appearance of any type of bifurcation (Fig. 9), because I_0 decreased after the injection of carbenoxolone. Thus, the qualitative structure of the dynamics of the individual IO neurons did not change from that of the control condition.

Having defined the dynamics of individual simulated IO neurons, the effect of gap junction coupling and fluctuating synaptic input were investigated. Both were found to contribute to the population dynamics of IO neurons. Namely, the gap junctions help synchronize the membrane potentials of coupled neurons, while the fluctuating inputs tend to desynchronize them (Fig. 8c, d). In the control condition (Fig. 8c), the membrane potential of each neuron mostly stays near the resting state, except when the magnitudes of

the independent fluctuations are large enough to cause the neurons produce action potentials. Mostly, the spikes of the different cells occur randomly with respect to each other; however, the attracting effect of gap junctions does lead to some synchronous spiking as indicated by arrows in Fig. 8c. In the picrotoxin condition (Fig. 8d), the resting state and the periodically spiking state coexist, and the fluctuating inputs induce switching between the two states. The attracting effect of gap junctions results in a tendency for the neurons to function as a group and therefore all stay together in one of the two attractors or switch states simultaneously. This results in network dynamics in which there are both highly rhythmic synchronous spiking states and random spiking states, as shown by the rasters of Fig. 4b.

3.4 Parameter dependence of CS activity

Picrotoxin and carbenoxolone induce alterations of parameter values that result in variations of the firing rate, rhythmicity, and synchrony of IO activity. How these characteristics of IO activity depend on the model's parameters is shown in Fig. 10.

If the gap junction conductance is fixed and the magnitude of constant input varies, firing rate, rhythmicity, and synchrony all increase with the magnitude of the constant input (Fig. 10a). The firing rate is also increased by the fluctuating input (Fig. 10b), which increases a tendency for the membrane potential to reach the spiking threshold. In the range below $\sigma \cong 1.4 \mu\text{A}/\text{cm}^2$, the dependency of CS activity on the fluctuating input (Figs. 10h-j) shows similarity to that on the constant input (Figs. 10e-g). The fluctuating input contributes the rhythmicity and synchrony in this range. In a relatively high fluctuating input range ($\sigma > 1.4 \mu\text{A}/\text{cm}^2$), on the other hand, the fluctuation disrupts the regularity and coincidence of spike timing and decreases the rhythmicity and synchrony.

On the other hand, if the gap junction conductance value is also allowed to vary, the dependence of these measures of IO activity on the input current is more complex (Figs. 10e-j). Synchrony monotonically increases with increasing coupling for any value of the constant input current, but changes of the firing rate and rhythmicity show a more

complicated dependence on the input current. Moreover, the changes in the firing rate and rhythmicity are highly correlated. In the range below $I_0 \cong 1.45 \mu\text{A}/\text{cm}^2$, the firing rate and the rhythmicity are suppressed by increasing the gap junction conductance (Fig. 10c). On the other hand, in a relatively high input current range ($I_0 > 1.45 \mu\text{A}/\text{cm}^2$), which corresponds to the picrotoxin condition, the firing rate and rhythmicity after initially decreasing, increase with increasing the gap junction conductance until $g_G \cong 10 \mu\text{S}/\text{cm}^2$ (Fig. 10d). With further increases in g_G the firing rate and rhythmicity gradually decline. Consistent with the model, a decrease in rhythmicity (in contrast to the increase with picrotoxin) was observed in some experiments in which lesions of the cerebellar nuclei (origin of the GABAergic input to the IO) were made, and high levels of synchrony (higher than those typically found with picrotoxin injections) were produced [Lang *et al.*, 1996].

The dependence of the firing rate on I_0 and the gap junction conductance can be understood from the viewpoint of dynamical systems theory. The fluctuating current is what triggers action potentials. In the range below $I_0 \cong 1.45 \mu\text{A}/\text{cm}^2$, the effect of gap junction coupling causes a decrease in the firing rate because coupled neurons attract their membrane potentials to each other and the fluctuating excitation randomly occurs in just a few cells at any moment. Thus, most cells are near the stable equilibrium (resting state), and therefore tend to suppress firing that would be caused by the fluctuating input in cells to which they are coupled. In contrast, in the upper range for $I_0 \cong 1.45 \mu\text{A}/\text{cm}^2$, the tendency for action potential generation is enhanced by an increase in gap junction conductance, because the fluctuating excitation occurs in several cells simultaneously, and membrane potentials of all of the cells tend to be attracted to spiking, leading to an increase in the firing rate.

4 Discussion

We have demonstrated that a gap junction-coupled system of two-variable conductance-based model neurons quantitatively reproduces the spatio-temporal dynamics of the spiking

patterns in the IO network. Furthermore, phase plane and bifurcation analyses were used to show that qualitative properties of the dynamical system can be shifted by the injection of drugs.

A simplified neuronal model was used in order to reduce the complexity of multi-ion channel dynamics. Nevertheless, some functional correspondence may exist between some of the model's conductances and those found in IO neurons. The model incorporated three major currents in its neurons: leak, depolarizing, and hyperpolarizing currents. The depolarizing current may act similarly to the low threshold calcium current of IO neurons in that it acted to depolarize the membrane potential toward firing threshold. Furthermore, the depolarizing current often triggered the activation of the hyperpolarizing current, because of the dependence of n on the membrane voltage (Eqs. (5)-(8)). Thus, the combined g_D and g_H mediated currents act to create depolarization-hyperpolarization sequences, which are phenomenologically similar to those displayed by IO neurons [Llinas & Yarom, 1986], even if the underlying mechanisms are somewhat distinct.

Evidence that the model captured essential aspects of IO network activity is that the model was able to generate data that were in good agreement with observations of CS activity under three distinct conditions: control, picrotoxin, and carbenoxolone. Moreover, changes in the model's parameters in the three conditions were generally consistent with what one would expect based on the pharmacological actions of the two drugs.

Picrotoxin is an antagonist of GABA_A receptors, which are the main receptors through which IO neurons are inhibited. Thus, the disinhibition caused by the picrotoxin injection should essentially be equivalent to an increase of the excitatory input magnitude. This is consistent with the results of our parameter estimation suggesting that the picrotoxin condition has an increased constant synaptic input compared to control (Table 1). Our results further indicate that the picrotoxin injection would increase the parameter value that corresponds to the gap junction conductance, which is in accord with previous experimental results [Lang *et al.*, 1996]. This dual action of GABA is consistent with the presence of GABAergic terminals both on the soma and main dendritic shafts of IO neurons, where

they are in a position to influence the overall excitability of the cell, and on dendritic spine heads, where they can selectively influence the effective coupling between IO neurons by controlling the conductance of the spine membrane, as described earlier (see Methods). It should be noted that the effects of picrotoxin can be produced in vivo by firing of Purkinje cells which inhibits cerebellar nuclei neurons sending GABAergic terminals to IO neurons, for example.

Carbenoxolone is an antagonist of gap junctions, which electrically couple the dendritic spines of neighboring neurons. Thus, the blockade of gap junctions by the carbenoxolone injection is consistent with our parameter estimation suggesting that the effective conductances among neurons are reduced by carbenoxolone (Table 1). The parameter estimation also suggests that the carbenoxolone injection reduces magnitudes of constant and fluctuating inputs. Although the interpretation of the reduction of these parameters in the carbenoxolone condition is not certain, the decrease in the magnitude of currents flowing through the gap junctions would also reduce the absolute level of the fluctuations in these currents, which could be the source of the reduction of the fluctuating input predicted by the model.

Further correspondence between the model and experimental data on the IO is that the sub-threshold oscillation observed in IO neurons can also be reproduced by the model. As shown in Fig. 8, even in a single neuron, the small perturbation caused by each current pulse triggers a damped oscillation of the membrane potential that lasts for several cycles. Although there are different possible mechanisms of sub-threshold oscillation [Manor *et al.*, 1997], our results suggest that the oscillation is a damping process towards the stable equilibrium of a subcritical-Hopf type model. The process can be viewed as a helical orbit around the stable equilibrium in the phase plane (Fig. 7a, b).

How the level of gap junction coupling affects the rhythmicity of CSs is unclear so far, but our results suggest that the rhythmicity is effected not only by the gap junction but also by changes in the constant and fluctuating input currents as shown in Fig. 10. The rhythmicity corresponds to repetitive firing with a period nearly equal to that of the limit cycle which is generated by the saddle-node bifurcation. It is worth noting that the model

could generate rhythmic CS activity in the absence of gap junction coupling between neurons, which is consistent with some experimental results, but not others [Bleasel & Pettigrew, 1992; Blenkinsop & Lang, 2006; Lampl & Yarom, 1997; Leznik & Llinas, 2005; Llinas & Yarom, 1986; Long *et al.*, 2002; Manor *et al.*, 1997; Marshall *et al.*, 2007; Placantonakis *et al.*, 2006].

The model also shows the clear dependence of CS synchrony on the gap junction coupling of IO neurons (Fig. 10). If there is no gap junction coupling, the fluctuating input current leads to completely asynchronous spiking of the neurons. However, in agreement with previous studies [Lang, 2002; Lang *et al.*, 1996], synchrony is markedly enhanced by an increase in the effective level of gap junction coupling among IO neurons.

The spatiotemporal patterns of CS activity shown in the Results section demonstrated the distinctive transition behavior between synchronous and asynchronous spiking states in the picrotoxin condition (Fig. 4b). Bimodal peaks in the minimal distance distribution in Fig. 4h also indicate the co-existence of these two states. The mechanism of the transition behavior can be explained by the characteristic structure of the neuron model. In the parameter region that corresponds to the picrotoxin condition, the neuron model has two attractors: the stable equilibrium point with the resting state and the stable limit cycle with the sustained spiking state that are easily switched by fluctuations, because a separatrix of these two states, which is formed by the unstable limit cycle, tends to be very close to the lower part of the stable limit cycle. When the state point on the stable limit cycle passes through this region, the state point can be easily trapped into the stable equilibrium. Conversely, the state point can easily exit from the trapped orbit around the stable equilibrium point by fluctuations because the position of the resting state, and hence parts of the orbit, are close to the separatrix.

Even if there is no gap junction coupling, these transitions can occur, but the times of these transitions in the network would not be synchronized. The gap junction coupling reduces differences in membrane potential among neurons, so that the resulting states of neurons in the network tend to be coherently biased either to the resting state or to the sustained spiking state, and so that the times of state transitions tend to be synchronized. It

seems, thus, that the gap junction coupling facilitates bistability at the network level. How such bistability contributes to functions of the olivocerebellar system is an open problem. One possible role of this intrinsic bistable state is to act as a short-term memory [Loewenstein *et al.*, 2005]. For example, a sufficiently large fluctuating input from IO afferents may trigger the synchronous state in IO, which can then be maintained for several hundred milliseconds. This maintained activity in the IO possibly affects cerebellar motor control and learning processes [Van Der Giessen *et al.*, 2008].

Here, we conclude that the dynamics of IO neurons are of the subcritical Hopf bifurcation type. This qualitative classification of neuronal dynamics should be tested using a higher dimensional model. Thus, the identification of the qualitative property of neuronal dynamics may contribute to the development of more realistic and higher-dimensional models. We also note that the use of the simple reduced model was the key to the success of this initial modeling with which we have begun to define the dynamical structure of the IO. We have also demonstrated that the dynamical properties of neurons can be estimated with spatiotemporal patterns of spikes. This approach should be applied for estimating the dynamical properties of other neural systems.

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Fig. 1. Spiking patterns of rat CS activity and statistical distributions that characterize the CS activity in the picrotoxin experiment. Raster plots of CS activity simultaneously recorded from 16 Purkinje cells before (a) and after (b) the injection of picrotoxin. In each plot, the vertical axes represent neurons, and the horizontal axes represent time. Each red dot indicates the time of a CS, and each row in the raster shows the CSs of one Purkinje cells. Typical 75 s durations are shown. Statistical distributions illustrate the characteristic CS activity before (c-f) and after (g-j) picrotoxin injection. (c, g) Auto-correlograms of CS activity from a typical Purkinje cell before and after picrotoxin injection. (d-f and h-j) show 16-channel averaged statistics of (d, h) auto-, (e, i) cross-correlograms, and (f, j) minimal distance distributions. The standard deviations are indicated with light blue bands. In the case of random spiking (the Poisson point process), the minimal distance distribution should be flat at the level indicated by the black dotted line and gray bar (mean \pm SD)

Fig. 2. Spiking patterns of rat CS activity and statistical distributions that characterize the CS activity in the carbenoxolone experiment. Raster plots of CS activity simultaneously recorded from 22 Purkinje cells before (a) and after (b) the injection of carbenoxolone. Statistical distributions illustrate the characteristic CS activity before (c-f) and after (g-j) carbenoxolone injection. (c, g) Auto-correlograms of CS activity from a typical Purkinje cell before and after carbenoxolone injection. (d-f and h-j) show 22-channel averaged statistics of (d, h) auto-, (e, i) cross-correlograms, and (f, j) minimal distance distributions.

Fig. 3. Gap junction coupled IO neurons and an effective conductance. (a) IO neurons are coupled via a gap junction, which locates on the spine membrane at the edge of the dendritic shaft. GABAergic synapses are connected on the dendritic shaft. The picrotoxin injection modulates the GABAergic conductance and leads change on the current flow on the dendritic shaft. (b) The equivalent circuit model of this gap junction coupled IO neurons. V_1 and V_2 are the membrane potential of each neuron. g_{GABA} , g_{GJ} , and g_{DS} are indicating conductances of the GABAergic synapses, the gap junction, and the dendritic shafts. The conductance of GABAergic synapses g_{GABA} varies with the picrotoxin injection, and leads to a change on the current flow on the gap junction I_{GJ} . (c) Simplified equivalent circuit that we used in the present model

Fig. 4. Simulation results obtained using optimized parameter values reproduce the spiking pattern of CS activity before (a and c-e) and after (b and f-g) picrotoxin injection. In the raster plots (a, b), the vertical axes of each plot indicate an index of 25 neurons. The horizontal axes indicate time. Each dot indicates the time of a CS. Typical 75s durations are shown. In the statistical distribution plots, blue bars and red curves show

experimental and simulation data, respectively. (c, f) Averaged auto-correlograms. (d, g) Averaged cross-correlograms. (e, h) The minimal distance distributions

Fig. 5. Simulation results obtained using optimized parameter values reproduce the spiking pattern of CS activity before (a and c-e) and after (b and f-g) carbenoxolone injection. (a, b) Raster plots. (c, f) Averaged auto-correlograms. (d, g) Averaged cross-correlograms. (e, h) The minimal distance distributions

Fig. 6. The parameter dependence of the summed difference function D_{total} (a) on the constant input and the gap junction and (b) on the fluctuating input and the gap junction.. (a, b) Control condition (c, d) Picrotoxin condition. The white circles show the estimated values of the parameters.

Fig. 7. Phase planes and bifurcation diagram in the picrotoxin experiment. (a, b) Phase planes describing the nonlinear dynamics of the model without fluctuating inputs and gap junction interactions under the constant input magnitudes that are estimated for the control condition (a) and the picrotoxin condition (b). Blue and green curves show nullclines that satisfy $\dot{V} = 0$ and $\dot{n} = 0$, respectively. Crossings of these curves, marked by red points, are the equilibrium points. Under both of the above two conditions, these equilibrium points are stable and correspond to the resting state. Gray arrows indicate the direction and the magnitude of the vector field of this dynamics. Black curves with arrows show the typical trajectories in the V-n space. (c) The bifurcation diagram showing a relation between the membrane potential and the magnitude of constant input, which describes the change in the dynamics. Red and blue dashed curves indicate stable and unstable equilibrium points. Red filled circles indicate the maximum and minimum values of the membrane potential in the stable limit cycle that corresponds to the periodically spiking state. Blue open circles indicate those of the unstable limit cycles. The two dashed vertical lines show input magnitudes that correspond to the control and picrotoxin conditions

Fig. 8. Membrane potential responses to current stimulations in simulations. Membrane potential time courses of 5s durations are shown. Horizontal dashed lines indicate the threshold potential that could mark spike occurrence times. (a, b) Responses of a single neuron (red traces) to current pulses with 50 ms width, which are superimposed on a constant input whose magnitude is specified for the two conditions (blue traces). (c, d) Typical responses of gap junction-coupled neurons ($N = 25$) with fluctuating input (10 of 25 neurons are plotted). A typical trace of a single neuron is plotted by the bold curve. Some synchronous spikes are indicated by arrows in c.

Fig. 9. Phase planes and the bifurcation diagram in the carbenoxolone experiment. Phase planes in (a) the control and (b) the carbenoxolone condition show the same qualitative structure, which consists of a stable equilibrium point (resting state). (c) The corresponding bifurcation diagram. Dashed vertical lines indicate the estimated magnitudes of the constant input.

Fig. 10. Parameter dependence of the firing rate, rhythmicity, and spike synchrony in simulations. (a-d) The mean and the standard deviation of the firing rate (black curves and gray bands), those of the rhythmicity (orange curves and orange band) and those of the synchrony of each pair (blue curves and blue bands) in the simulations. (a) Dependence on the magnitude of the constant input, and (b) that of the fluctuating input. (c, d) Dependence on the coupling of the gap junction in (c) a relatively low input current range as in the control condition ($I_0 = 1.35 \mu\text{A}/\text{cm}^2$), and in (d) a high input current range that corresponds to the picrotoxin condition ($I_0 = 1.55 \mu\text{A}/\text{cm}^2$). (e-j) Dependence of (e, h) the firing rate, (f, i) the rhythmicity, and (g, j) the synchrony, respectively, on the two parameters: namely, the constant input current and the conductance of gap junction(e-g), and the fluctuating input and the conductance of gap junction(h-j). White dashed lines indicate the parameter values of a-d. The white point with mark “c” indicates the parameter values specified with the control condition

Table 1 Estimated parameter values for the model with two experiments.

For the time constant of variable n , a common value was used for two conditions. Parameters that correspond to the gap junction, the magnitude of the constant input, and that of the fluctuating input were obtained for each condition.

Experiment	injection of drug	Time	Gap junction	Constant	Fluctuating
		constant of variable n τ_n (ms)	coupling g_G ($\mu\text{S}/\text{cm}^2$)	input I_0 ($\mu\text{A}/\text{cm}^2$)	input σ ($\mu\text{A}/\text{cm}^2$)
Picrotoxin	Before	49.72	5.19	1.36	0.56
	(After)		(6.51)	(1.64)	(0.33)
Carbenoxolone	Before	25.76	23.9	1.24	1.45
	(After)		(5.14)	(0.78)	(1.22)

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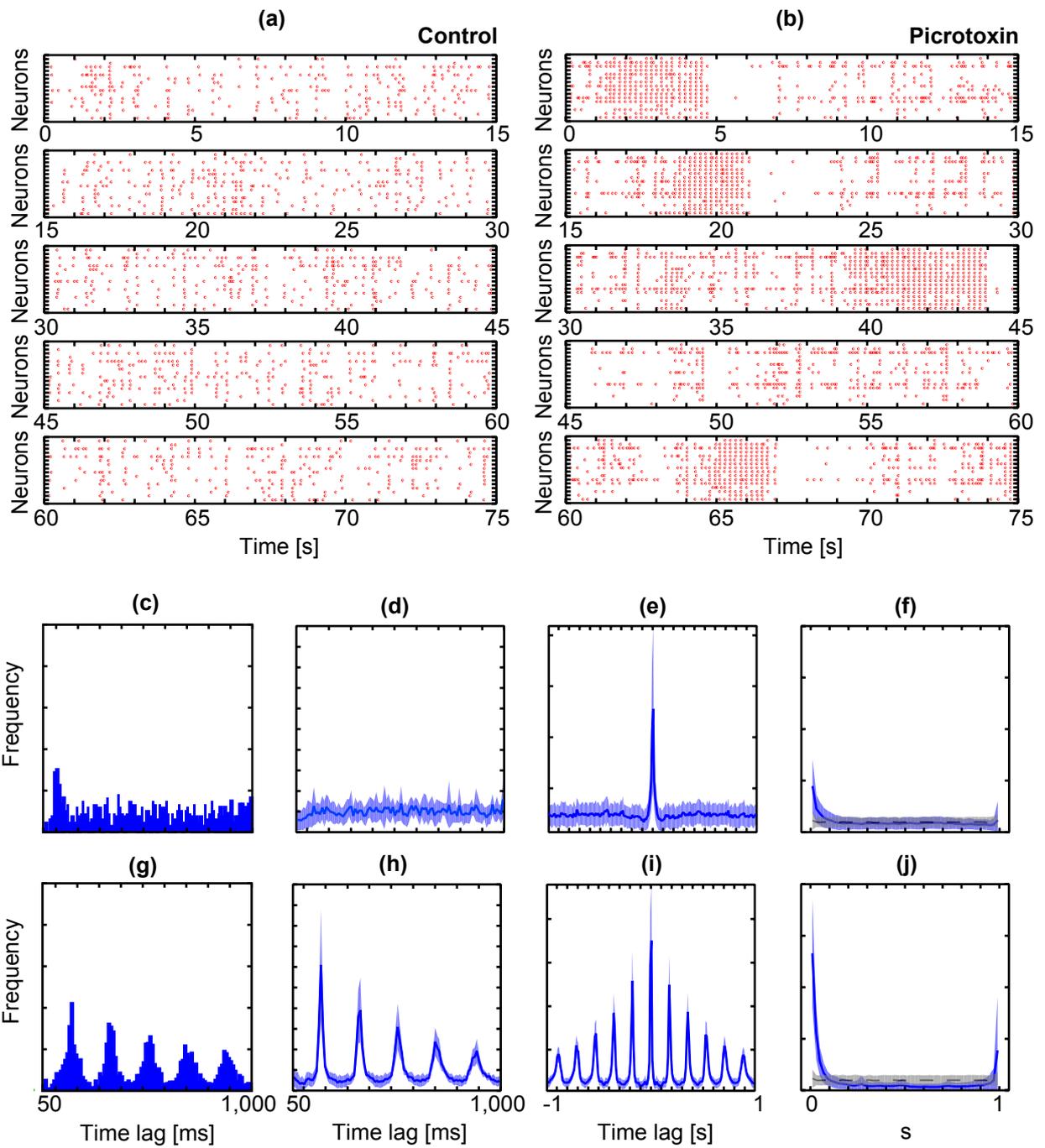


Figure 1

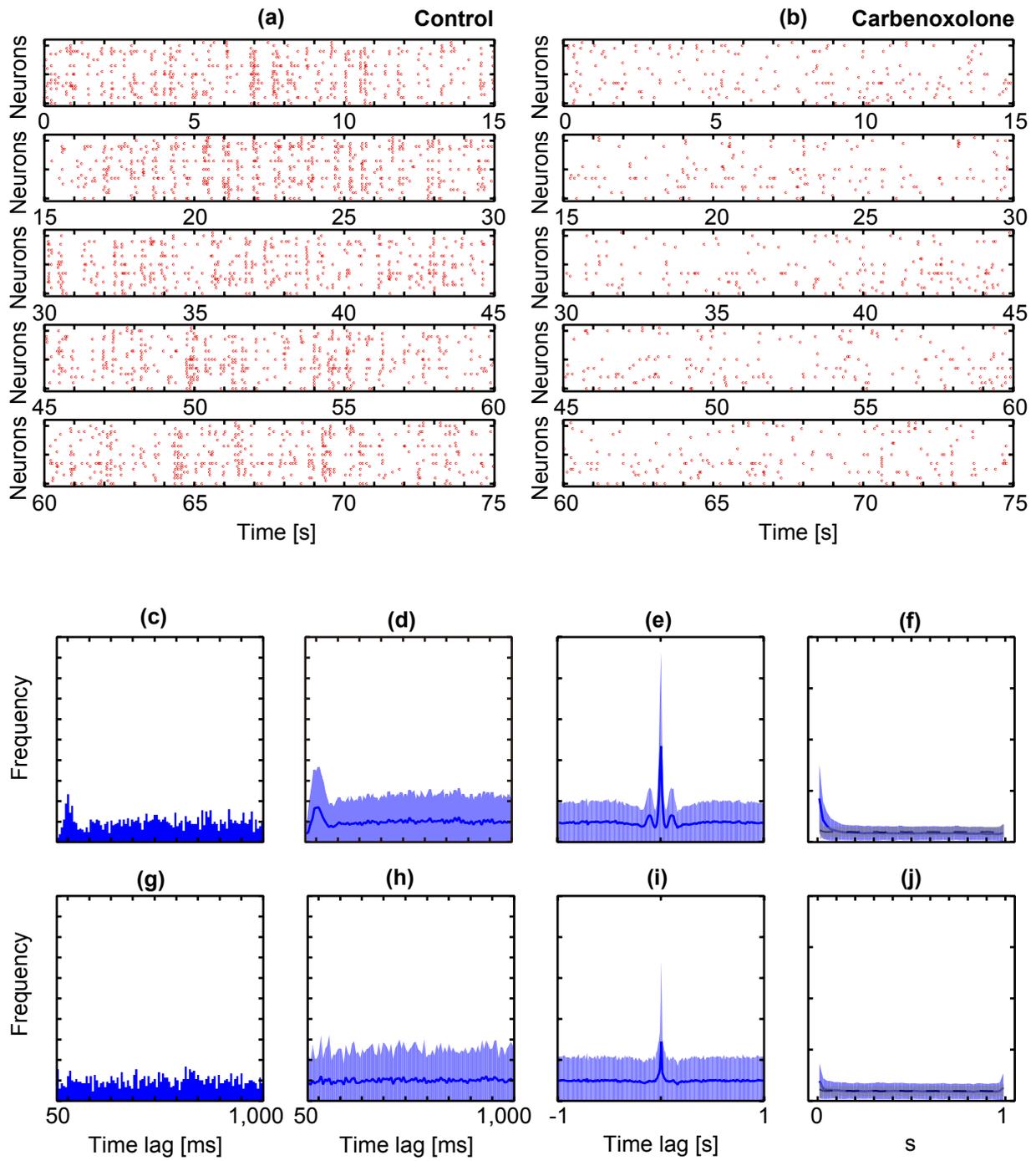


Figure 2

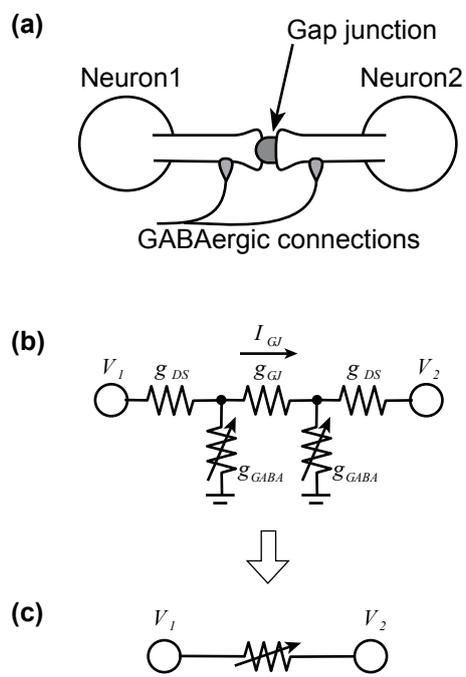


Figure 3

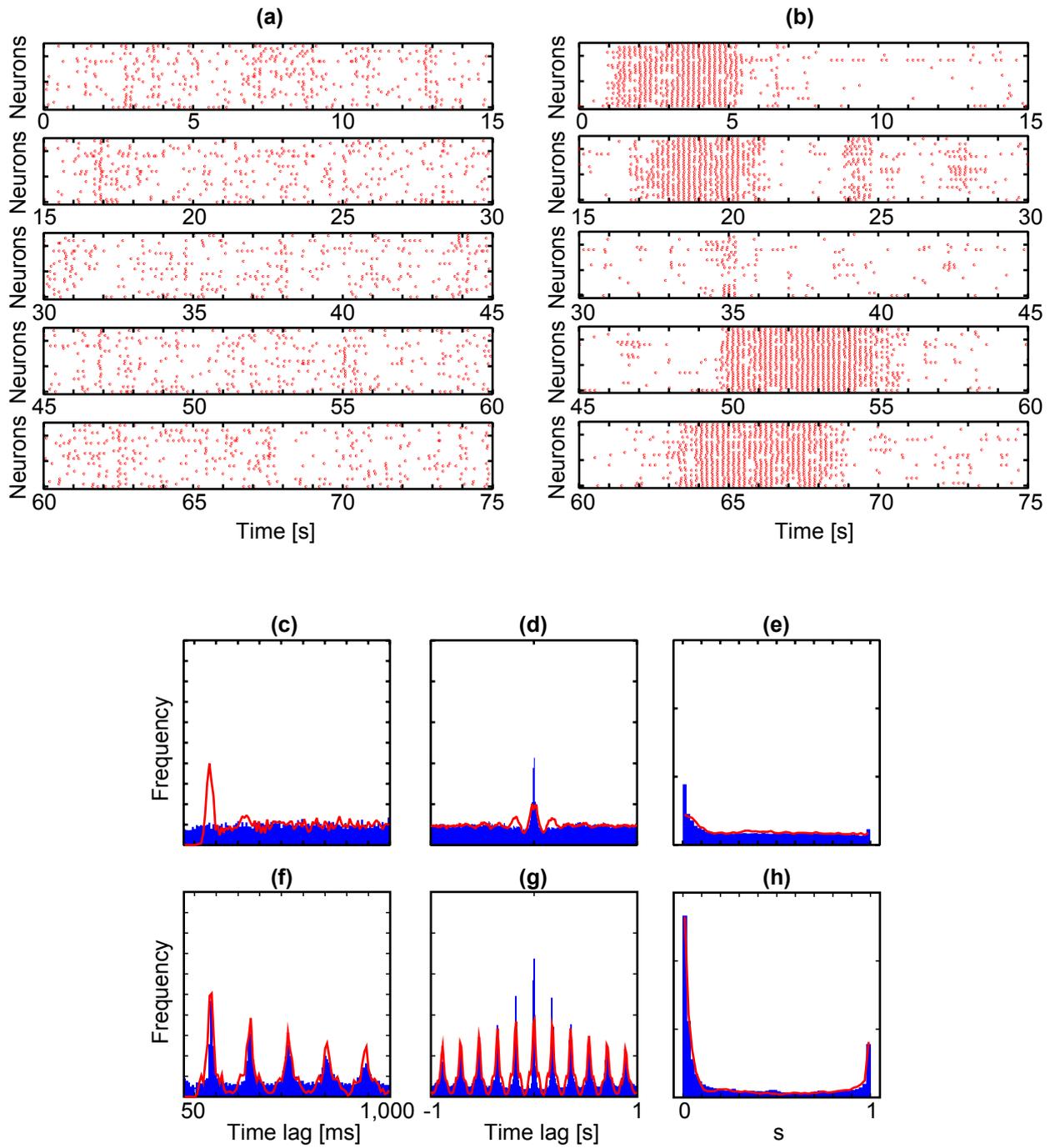


Figure 4

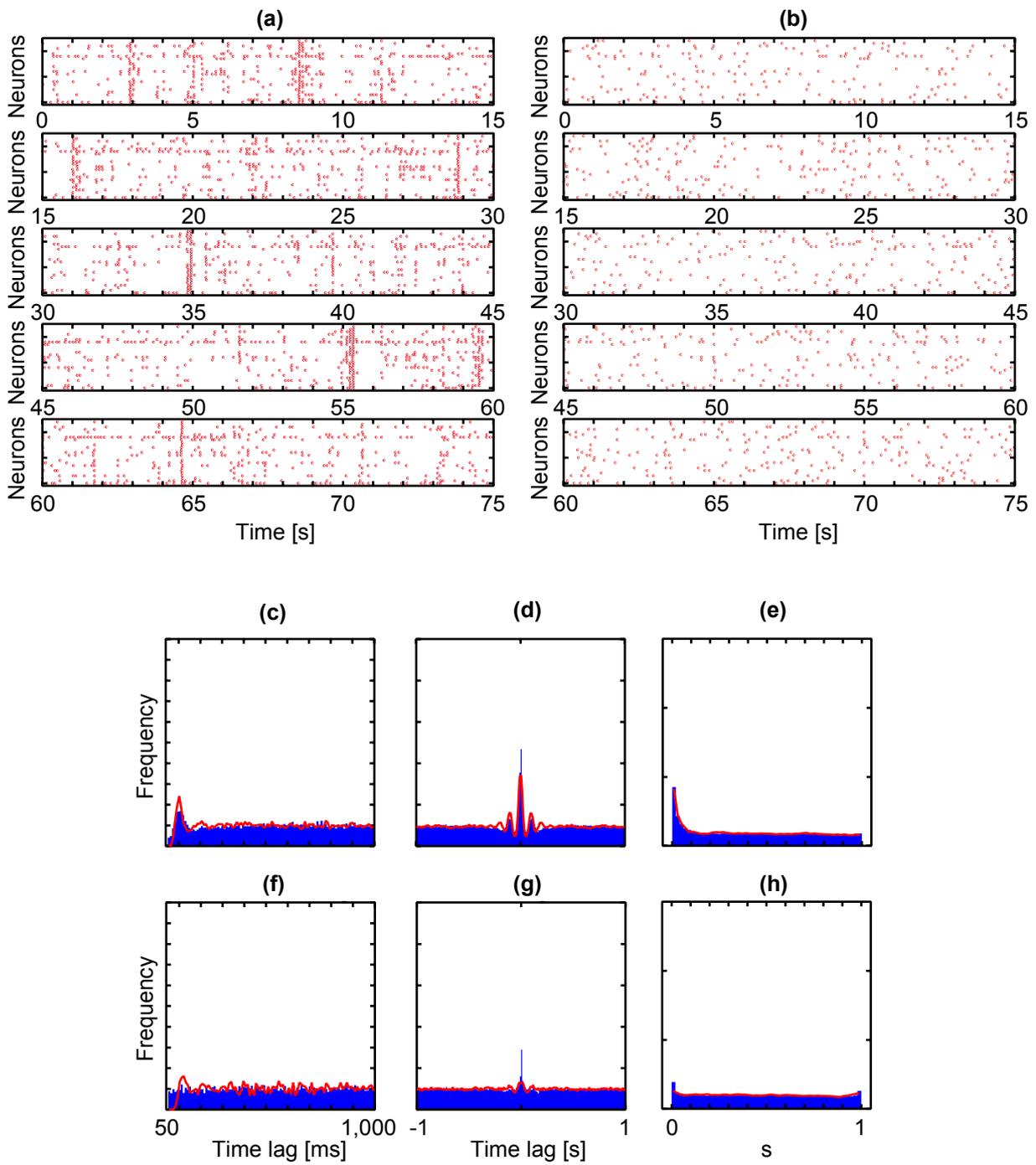


Figure 5

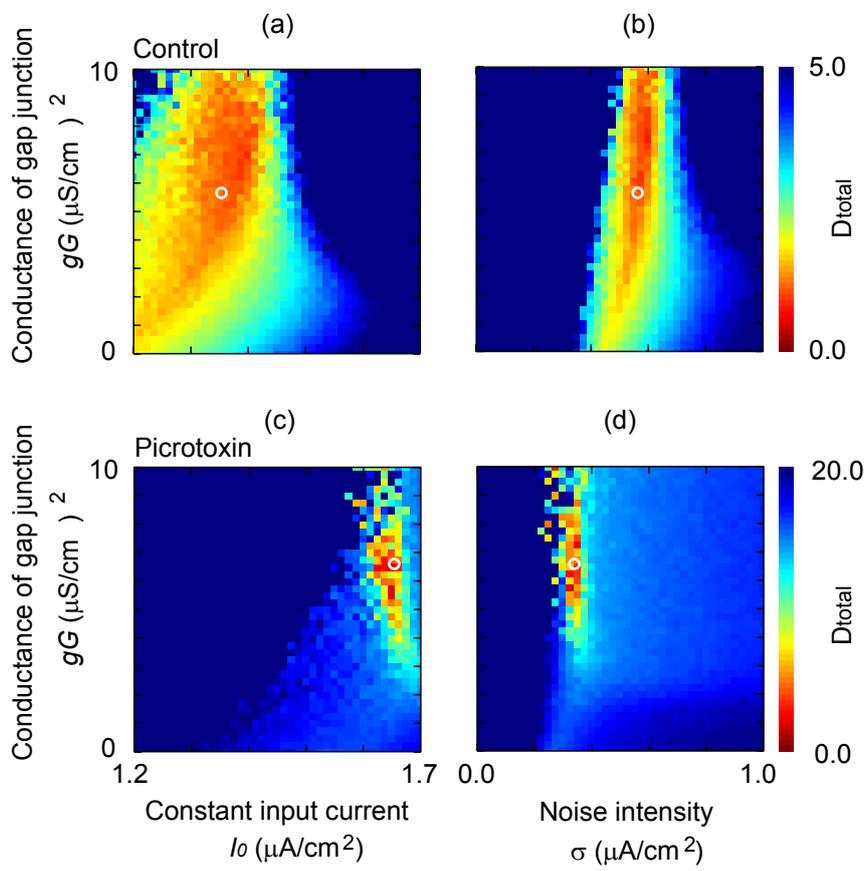


Figure 6

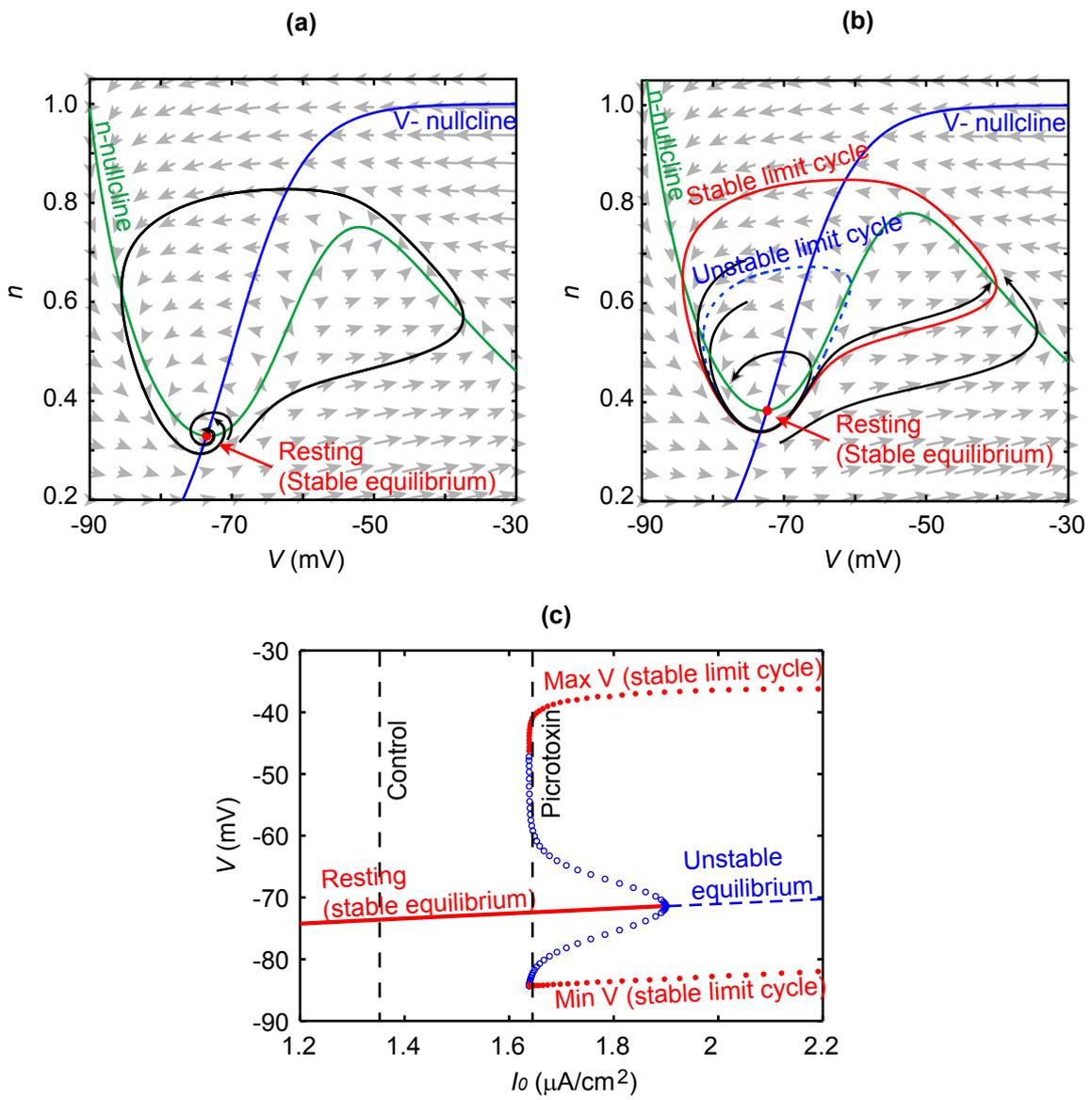


Figure 7

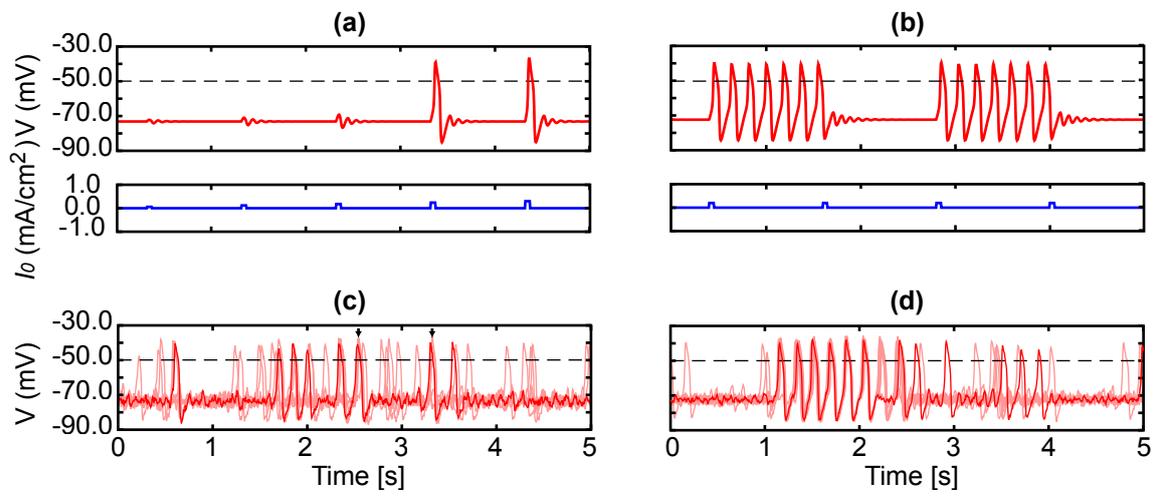


Figure 8

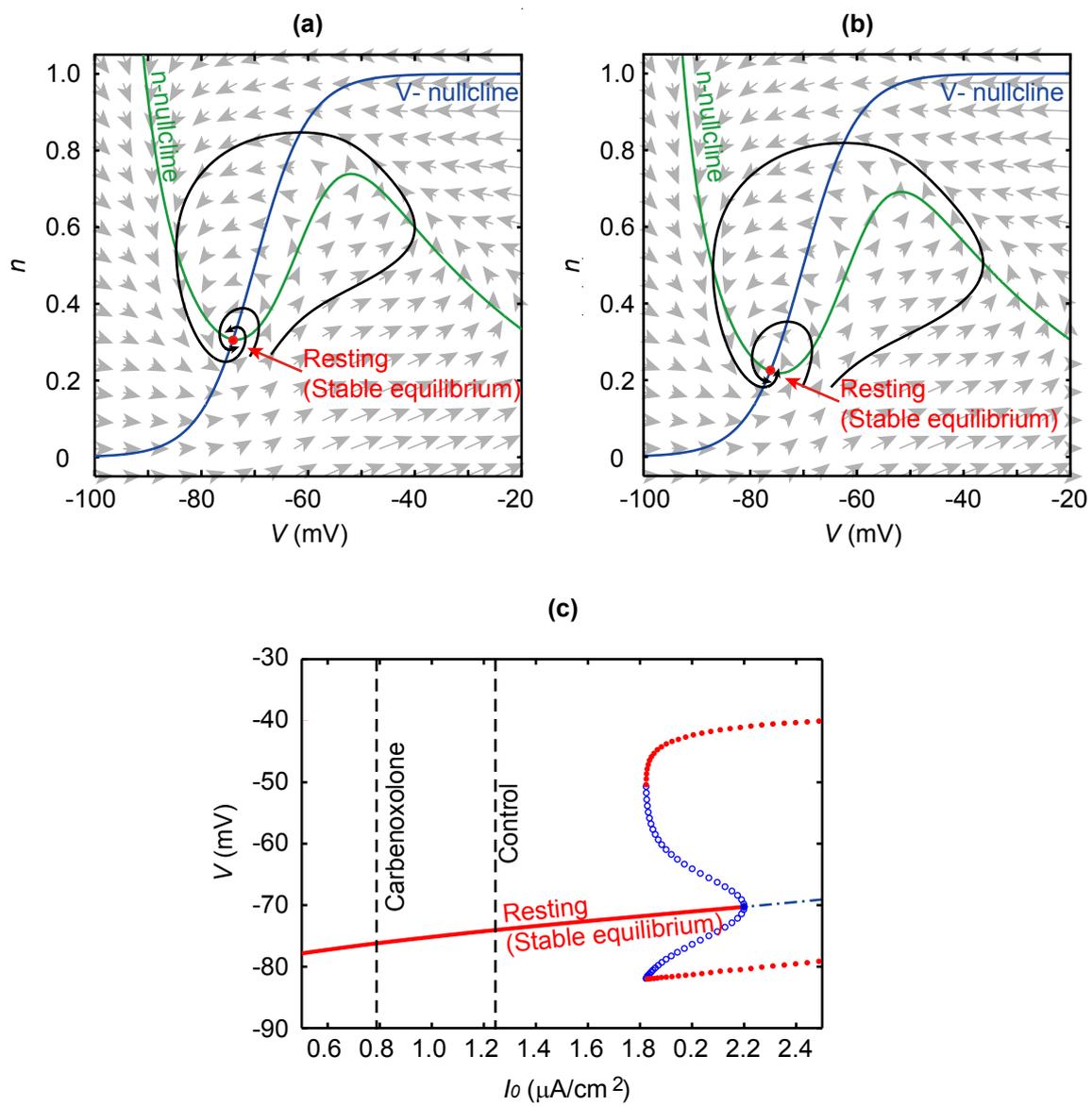


Figure 9

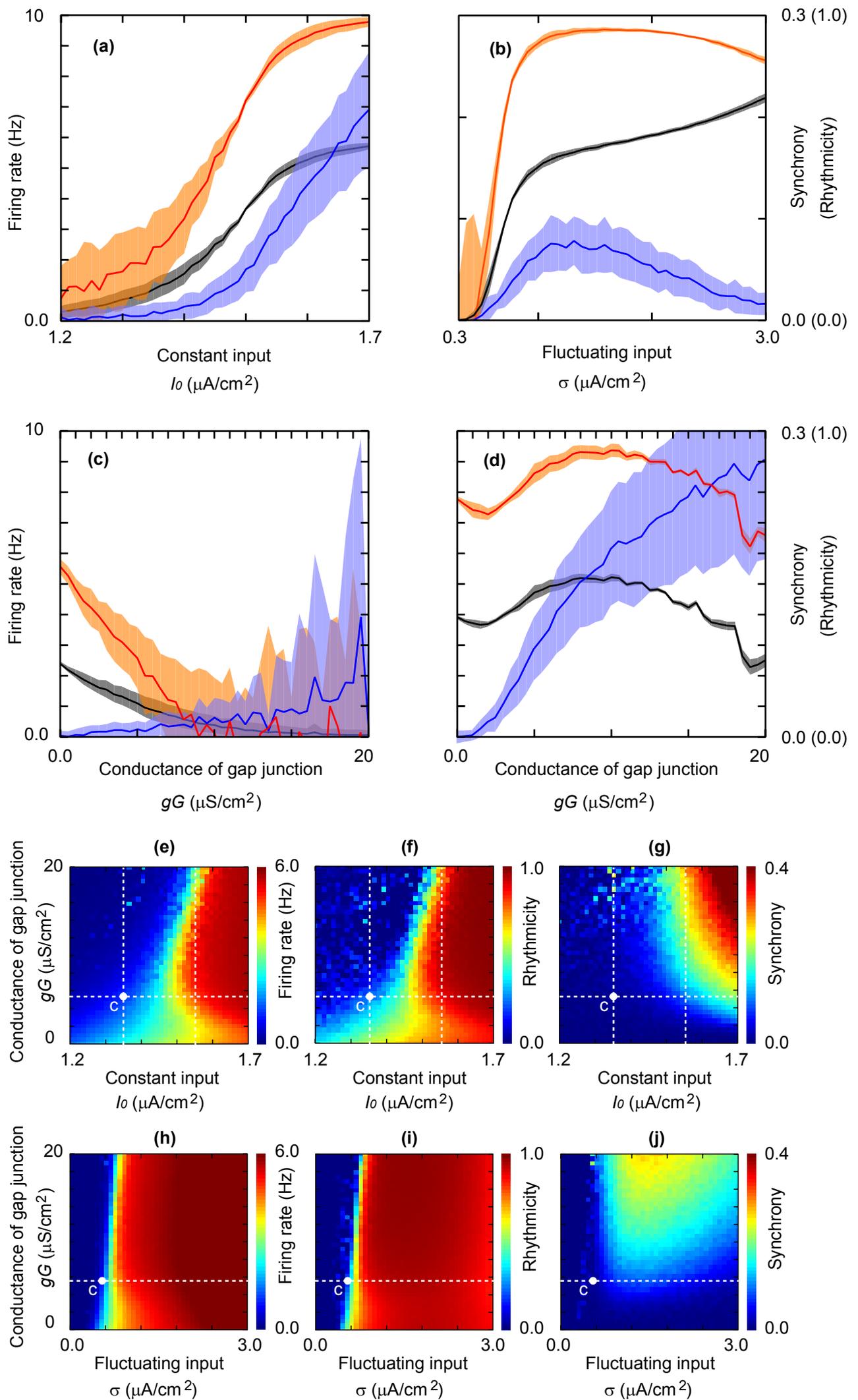


Figure 10